# Polymorphic P Systems: How Much Win? 

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## Polymorphic P Systems

[A. Alhazov, S.Ivanov, Yu. Rogozhin, 2010]

The Skin


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Contents

- multiset


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Pairs of membranes

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Define the rule $a \rightarrow a a$


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Rules modify rules

Define the rule $a \rightarrow a a$


Generating $n$ !

$$
\begin{gathered}
a_{1 L} \square_{1 R} \\
2: b \rightarrow b d \\
3: b \rightarrow\left(c, i n_{1 L}\right) \\
4: d \rightarrow\left(a, i n_{1 R}\right) \\
a b d
\end{gathered}
$$

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Generating $n$ !

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\begin{gathered}
a_{1 L} a^{3} \\
2: b \rightarrow b d \\
3: b \rightarrow\left(c, i n_{1 L}\right) \\
4: d \rightarrow\left(a, i n_{1 R}\right) \\
a^{2} b d
\end{gathered}
$$

Generating $n$ !

$$
\begin{gathered}
a_{1 L} a_{1 R} \\
2: b \rightarrow b d \\
3: b \rightarrow\left(c, i n_{1 L}\right) \\
4: d \rightarrow\left(a, i n_{1 R}\right) \\
a^{6} b d
\end{gathered}
$$

Generating $n$ !

$$
\begin{gathered}
a_{1 L} a_{1 R} \\
2: b \rightarrow b d \\
3: b \rightarrow\left(c, i n_{1 L}\right) \\
4: d \rightarrow\left(a, i n_{1 R}\right) \\
a^{24}
\end{gathered}
$$

## Superexponential Growth

Skin contents
0 . $a$


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Skin contents
0 . a

1. $a^{2}$
2. $a^{8}$


## Superexponential Growth

Skin contents
0 . a

1. $a^{2}$
2. $a^{8}$
3. $a^{64}$


## Superexponential Growth



## Superexponential Growth

Skin contents
0 . $a$

1. $a^{2}$
2. $a^{8}$
3. $a^{64}$
4. $a^{1024}$
n. $a^{2^{\frac{n(n+1)}{2}}}$


## [UMHPOMTMORFHBCB



## How Much Win?



## Intuitive Reasoning

## Efficient solutions beyond $P$



Fast exhaustive search

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\Downarrow \quad \text { (unless } P=N P)
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Fast exhaustive search

- Adleman's experiment
- SAT with P systems


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## Efficient solutions beyond $P$

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Fast exhaustive search

- Adleman's experiment
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## Candidates must be tracked

## Questions

Polymorphism can replicate symbols a lot

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Polymorphism can replicate symbols a lot
How about identities?

- interpretations of symbols


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If No, how much speed-up?

## Relevance for HPC

## Program = Data

- Programs working in parallel on programs :-)


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## Easier implementable?

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## Program = Data

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# Easier implementable? 

- easily?


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Polymorphism can replicate symbols a lot
How about identities?

- interpretations of symbols

Conjecture: No.

- identity traded for quantity

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